



$$= \frac{6}{1+3} (-1 - \sqrt{3}i) = \frac{3}{2} (-1 - \sqrt{3}i) = 3 \left( -\frac{1}{2} - \frac{\sqrt{3}}{2}i \right)$$

$$= 3 \left[ \cos \left( \frac{2\pi}{3} \right) + i \sin \left( \frac{2\pi}{3} \right) \right]$$

එබැවින්  $\frac{3}{z^2}$  හි නියතය 3 දූර්ග විෂයය  $-\frac{2\pi}{3}$

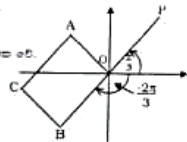
p ලක්ෂ්‍යය x කිවිසිල කඩිනම් කිරීමට සාධකය

$$POB = \left| \text{Arg } Z - \text{Arg} \left( \frac{3}{z^2} \right) \right|$$

$$= \left| \frac{\pi}{3} - \left( -\frac{2\pi}{3} \right) \right|$$

$$= \pi$$

P, O, B ලක්ෂ්‍ය



C කේන්ද්‍රයේ කිරීමට සාධකය

$$= 2x^2 + \frac{3}{x^2}$$

$$= -1 + \sqrt{3}i - \frac{3}{2} (1 + \sqrt{3}i)$$

$$= -\frac{5}{2} - \frac{\sqrt{3}}{2}i$$

$$CO \text{ හි දිග} = \sqrt{\frac{25}{4} + \frac{3}{4}} = \frac{\sqrt{28}}{2} = \sqrt{7}$$

$$AB \text{ හි දිග} = \left| 2x^2 - \frac{3}{x^2} \right|$$

$$= \left| -1 + \sqrt{3}i + \frac{3}{2} + \frac{3\sqrt{3}}{2}i \right|$$

$$= \left| \frac{1}{2} + \frac{5\sqrt{3}}{2}i \right|$$

$$= \sqrt{\frac{1}{4} + \frac{75}{4}} = \sqrt{19}$$

05. (a)  $y = e^{-ix} (\cos 2x + \sin 2x)$

$$\frac{dy}{dx} = e^{-ix} (-2 \sin 2x + 2 \cos 2x)$$

$$= e^{-ix} (-3 \sin 2x + \cos 2x)$$

$$\frac{dy}{dx} + y = -3e^{-ix} \sin 2x + e^{-ix} \cos 2x$$

$$= 2e^{-ix} \cos 2x - 2e^{-ix} \sin 2x$$

$$= 2e^{-ix} (\cos 2x - \sin 2x)$$

$$\frac{d^2y}{dx^2} + \frac{dy}{dx} = 2e^{-ix} (-2 \sin 2x - 2 \cos 2x)$$

$$= 2(\cos 2x - \sin 2x) (-e^{-ix})$$

$$= -4e^{-ix} (\sin 2x + \cos 2x)$$

$$= -2e^{-ix} (\cos 2x - \sin 2x)$$

$$= -4y - \left( \frac{dy}{dx} + y \right)$$

$$\frac{d^2y}{dx^2} + 2 \frac{dy}{dx} + 5y = 0 \quad p = 2 \quad q = 2$$

$$\frac{d^2y}{dx^2} + 2 \frac{dy}{dx} + 5y = 0$$

$$y(0) = 1, \left( \frac{dy}{dx} \right)_{x=0} = 1$$

$$\left( \frac{d^2y}{dx^2} \right)_{x=0} = -2 \left( \frac{dy}{dx} \right)_{x=0} - 5y(0) = -7$$

$$\left( \frac{d^2y}{dx^2} \right)_{x=0} = -2 \left( \frac{d^2y}{dx^2} \right)_{x=0} - 5 \left( \frac{dy}{dx} \right)_{x=0}$$

$$= 14 - 5 = 9$$

(b) ඉදිරි සාදන ක්‍රමයට අනුව  $x$  cm හි දී  $y$  cm පළල වේ.

එවිට කේන්ද්‍රයේ පළල හි දී  $y$  cm පළල වේ.

$(x + 12)$  cm හි  $(y + 16)$  cm පළල වේ.

එවිට කේන්ද්‍රයේ විෂයය  $xy = 972$  වේ.

$$A(x) = (x + 12) \left( \frac{972}{x} + 16 \right)$$

$$A'(x) = (x + 12) \left( -\frac{972}{x^2} \right) + \left( \frac{972}{x} + 16 \right)$$

$$A'(x) = -\frac{12 \times 972}{x^2} + 16$$

$$= \frac{16x^2 - 16 \times 27^2}{x^2}$$

$$= \frac{16(x^2 - 27^2)}{x^2}$$

$$A'(x) = 0 \text{ වී } x = \pm 27$$

x හි ධන අගය  $x = 27$

$$\therefore A'(x) = \frac{16(x - 27)(x + 27)}{x^2}$$

$0 < x < 27$  වී  $A'(x) < 0$

$27 < x$  වී  $A'(x) > 0$

$\therefore A(x)$   $x = 27$  වී උපරිමයක් ගනී.

කේන්ද්‍රයේ විෂයය අවම වී  $x = 27$  හි අගයය  $y = \frac{972}{27} = 36$

$\therefore$  කේන්ද්‍රයේ ඉඩ  $39 \text{ cm} \times 52 \text{ cm}$  වේ.

06. (a)  $I = \int_{-1}^{23} \frac{1}{(x+1)\sqrt{2x+3}} dx$

$t = \sqrt{2x+3}$  ලෙස ගනිමු.

එවිට  $t^2 = 2x+3 \Rightarrow 2t dt = 2 dx \Rightarrow dx = t dt$

යම්  $x+1 = \frac{t^2-3}{2} + 1 = \frac{t^2-1}{2}$  වේ.

$x = -1$  වී  $t = 1$  වේ.  $x = 23$  වී  $t = 7$  වේ.

$I = \int_1^7 \frac{2 dt}{t^2-1} = \int_1^7 \frac{2 dt}{(t-1)(t+1)}$

$$= 2 \int_1^7 \left( \frac{1/2}{t-1} - \frac{1/2}{t+1} \right) dt$$

$$= \int_1^7 \frac{dt}{t-1} - \int_1^7 \frac{dt}{t+1}$$

$$= \left[ \ln |t-1| \right]_1^7 - \left[ \ln |t+1| \right]_1^7$$

$$= \ln \frac{6}{4} - \ln \frac{8}{6}$$

$$= \ln \frac{9}{8}$$

(b)  $J = \int e^{3x} \cos 4x dx$

$$= \int e^{3x} \frac{d}{dx} \left[ \frac{\sin 4x}{4} \right] dx$$

$$= e^{3x} \frac{\sin 4x}{4} - \int \sin 4x \frac{d}{dx} (e^{3x}) dx$$

$$= e^{3x} \frac{\sin 4x}{4} - \int e^{3x} \sin 4x dx$$

$$= \frac{1}{4} e^{3x} \sin 4x - \frac{3}{4} \int e^{3x} \frac{d}{dx} \left( \frac{\cos 4x}{4} \right) dx$$

$$= \frac{1}{4} e^{3x} \sin 4x - \frac{3}{4} \left( \frac{e^{3x} \cos 4x}{4} \right)$$

$$= \frac{1}{4} e^{3x} \sin 4x - \frac{3}{16} e^{3x} \cos 4x$$

$$= \frac{1}{4} e^{3x} \sin 4x + \frac{3}{16} e^{3x} \cos 4x$$

$$= \frac{9}{16} \int e^{3x} \cos 4x dx$$

$$16J = 4e^{3x} \sin 4x + 3e^{3x} \cos 4x - 9J$$

$$25J = e^{3x} [4 \sin 4x + 3 \cos 4x]$$

$$J = \frac{e^{3x}}{25} [4 \sin 4x + 3 \cos 4x]$$

$$\therefore \int e^{3x} \cos 4x dx = \frac{e^{3x}}{25} [4 \sin 4x + 3 \cos 4x] + C$$

(c)  $\int \sin^4 2x dx = \int \left[ \frac{1}{2} (1 - \cos 4x) \right]^2 dx$

$$= \frac{1}{4} \int (1 - 2 \cos 4x + \cos^2 4x) dx$$

$$= \frac{1}{4} \int (1 - 2 \cos 4x + \frac{1}{2} (1 + \cos 8x)) dx$$

$$= \frac{1}{8} \int (3 - 4 \cos 4x + \cos 8x) dx$$

$$= \frac{3}{8} x - \frac{4 \sin 4x}{4 \times 8} + \frac{\sin 8x}{8 \times 8} + C$$

$$= \frac{3x}{8} - \frac{\sin 4x}{8} + \frac{\sin 8x}{64} + C$$

07. u හි v සිටින කේන්ද්‍රයේ ගිණි දී එවැනි අනුක්‍රමයක් m වී දී යයි.

එවිට  $y = m(x - 5)$  හි  $y = m(x + 5)$  වේ.

$$y = mx - 5m$$

$$3y + 4x = 25 \Rightarrow x = \frac{25 + 15m}{4 + 3m}$$

$$y = \frac{5m}{4 + 3m}$$

එවිට P =  $\left( \frac{25 + 15m}{4 + 3m}, \frac{5m}{4 + 3m} \right)$

එවිට Q =  $\left( \frac{25 + 15m}{4 + 3m}, \frac{5m}{4 + 3m} \right)$

එවිට PQ =  $\left( \frac{25 + 15m}{4 + 3m}, \frac{5m}{4 + 3m} \right)$

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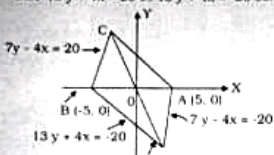
එවිට PQ =  $\left( \frac{25 + 15m}{4 + 3m}, \frac{5m}{4 + 3m} \right)$

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එවිට PQ =  $\left( \frac{25 + 15m}{4 + 3m}, \frac{5m}{4 + 3m} \right)$

එනම්  $13y + 4x = 20$  හා  $13y + 4x = -20$  වේ.



මෙම රේඛාවලට සමාන්තරව පවතින රේඛාවක  $y = 0$  හි  
අභ්‍යන්තර දිශාව (0, 0) වේ.

අනෙක් දිශාව

අභ්‍යන්තර දිශාව  $7y - 4x + 20 + \lambda(13y + 4x + 20) = 0$

වලට වේ.

මෙය සමීකරණයකට පත් කළ විට

$$\begin{cases} 7y - 4x + 20 + \lambda(13y + 4x + 20) = 0 \\ 3y + 4x = 0 \end{cases} \quad \lambda = -1$$

$$7y - 4x + 20 - 13y - 4x - 20 = 0 \Rightarrow -6y - 8x = 0 \Rightarrow 3y + 4x = 0$$

$$\therefore C = \left( \frac{3}{2}, -\frac{3}{2} \right)$$

ACBD සමාන්තරකෝණී චතුරස්‍රය

$$= 2 \times \text{Area } \triangle ABC$$

$$= 2 \times \frac{1}{2} \times 10 \times 10$$

$$= 200 \text{ ටී.මී.}^2$$

04.  $S_1 = x^2 + y^2 - 2 = 0$

$$S_2 = x^2 + y^2 + 3x + 3y - 8 = 0$$

$$S_1 = 0; \text{ මධ්‍යස්ථ ලක්ෂ්‍ය } C_1 = (0, 0)$$

$$\text{රේඩියස් } r_1 = \sqrt{0^2 + 0^2 + 2} = \sqrt{2}$$

$$S_2 = 0; \text{ මධ්‍යස්ථ ලක්ෂ්‍ය } C_2 = \left( -\frac{3}{2}, -\frac{3}{2} \right)$$

$$\text{රේඩියස් } r_2 = \sqrt{\left( \frac{3}{2} \right)^2 + \left( \frac{3}{2} \right)^2 + 8} = \frac{5\sqrt{2}}{2}$$

$$\therefore C_1C_2 = \sqrt{\left( \frac{3}{2} \right)^2 + \left( \frac{3}{2} \right)^2} = \frac{3\sqrt{2}}{2}$$

$$r_2 - r_1 = \frac{5\sqrt{2}}{2} - \sqrt{2} = \frac{3\sqrt{2}}{2}$$

$$r_2 - r_1 = C_1C_2 \text{ වේ.}$$

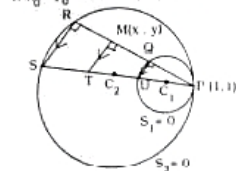
$$S_1 = 0 \text{ හා } S_2 = 0 \text{ අන්තර්ප්‍රේෂණය වන්නේ එකම ලක්ෂ්‍යයකි.}$$

$$\therefore 3x_0 + 3y_0 - 6 = 0 \Rightarrow x_0 + y_0 = 2$$

මෙම රේඛාවලට සමාන්තරව පවතින රේඛාවක  $y = x$   
අභ්‍යන්තර දිශාව වේ.

$$\therefore y_0 = x_0$$

$$\therefore x_0 + y_0 = 1 \Rightarrow P = (1, 1) \text{ වේ.}$$



P, C<sub>1</sub>, C<sub>2</sub> ලක්ෂ්‍යයන් සහ මධ්‍යස්ථ ලක්ෂ්‍යය U හි S හි  
මධ්‍යස්ථ ලක්ෂ්‍යය S<sub>1</sub> = 0 හා S<sub>2</sub> = 0 අන්තර්ප්‍රේෂණය වන්නේ එකම ලක්ෂ්‍යයකි.

$$S = (x_1, y_1) \text{ ලක්ෂ්‍යය වේ.}$$

$$\text{එවිට } \frac{x_1 + 1}{2} = -\frac{3}{2} \text{ හා } \frac{y_1 + 1}{2} = -\frac{3}{2} \text{ වේ.}$$

$$x_1 = -4, y_1 = -4 \Rightarrow S = (-4, -4)$$

මෙම U = (-1, -1) හි SU හි මධ්‍යස්ථ ලක්ෂ්‍යය T වේ.

$$T = \frac{-4 + (-1)}{2}, \frac{-4 + (-1)}{2} = \left( -\frac{5}{2}, -\frac{5}{2} \right)$$

QR හි මධ්‍යස්ථ ලක්ෂ්‍යය M(x, y) වේ.

TP රේඛාවේ දිශාව සහ M හි ස්ථානය

$$TP \text{ හි මධ්‍යස්ථ ලක්ෂ්‍යය } = \left( \frac{3}{4}, \frac{3}{4} \right)$$

$$\text{එවිට } \left( x + \frac{3}{4} \right)^2 + \left( y + \frac{3}{4} \right)^2 = \left( \frac{3}{4} \right)^2 + \left( \frac{3}{4} \right)^2$$

$$= \left( \frac{3}{4} - 1 \right)^2 + \left( \frac{3}{4} - 1 \right)^2$$

$$= \left( -\frac{1}{4} \right)^2 + \left( -\frac{1}{4} \right)^2$$

$$= \frac{1}{8} + \frac{1}{8} = \frac{1}{4}$$

$$\Rightarrow x^2 + y^2 + \frac{3}{2}x + \frac{3}{2}y + \frac{9}{8} = \frac{1}{4}$$

$$\Rightarrow x^2 + y^2 + \frac{3}{2}x + \frac{3}{2}y + \frac{9}{8} - \frac{2}{8} = 0$$

$$\Rightarrow x^2 + y^2 + \frac{3}{2}x + \frac{3}{2}y + \frac{7}{8} = 0$$

$$\therefore M \text{ හි මධ්‍යස්ථ ලක්ෂ්‍යය } = \left( -\frac{3}{4}, -\frac{3}{4} \right)$$

$$x^2 + y^2 + \frac{3}{2}x + \frac{3}{2}y + \frac{7}{8} = 0$$

$$\Rightarrow x^2 + y^2 + \frac{3}{2}x + \frac{3}{2}y + \frac{7}{8} = 0$$

$$\Rightarrow x^2 + y^2 + \frac{3}{2}x + \frac{3}{2}y + \frac{7}{8} = 0$$

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$$(b) \sin \frac{\pi}{12} = \sin \left( \frac{\pi}{4} - \frac{\pi}{6} \right)$$

$$= \sin \frac{\pi}{4} \cos \frac{\pi}{6} - \cos \frac{\pi}{4} \sin \frac{\pi}{6}$$

$$= \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{2}} \cdot \frac{1}{2}$$

$$= \frac{\sqrt{3} - 1}{2\sqrt{2}}$$

$$\cos \frac{\pi}{12} = \cos \left( \frac{\pi}{4} - \frac{\pi}{6} \right)$$

$$= \cos \frac{\pi}{4} \cos \frac{\pi}{6} + \sin \frac{\pi}{4} \sin \frac{\pi}{6}$$

$$= \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \cdot \frac{1}{2}$$

$$= \frac{\sqrt{3} + 1}{2\sqrt{2}}$$

$$\frac{1 - \cos 2x}{\sin 2x} = \frac{2 \sin^2 x}{2 \sin x \cos x} = \tan x$$

$$\tan \frac{\pi}{24} = \frac{1 - \cos \frac{\pi}{12}}{\sin \frac{\pi}{12}}$$

$$= \frac{1 - \frac{\sqrt{3} + 1}{2\sqrt{2}}}{\frac{\sqrt{3} - 1}{2\sqrt{2}}}$$

$$= \frac{2\sqrt{2} - \sqrt{3} - 1}{\sqrt{3} - 1}$$

$$= \frac{(2\sqrt{2} - \sqrt{3} - 1)(\sqrt{3} + 1)}{(\sqrt{3} - 1)(\sqrt{3} + 1)}$$

$$= \frac{(2\sqrt{2} - \sqrt{3} - 1)(\sqrt{3} + 1)}{3 - 1}$$

$$= \frac{(2\sqrt{2} - \sqrt{3} - 1)(\sqrt{3} + 1)}{2}$$

$$= \frac{2\sqrt{2}(\sqrt{3} + 1) - \sqrt{3}(\sqrt{3} + 1) - (\sqrt{3} + 1)}{2}$$

$$= \frac{2\sqrt{2}\sqrt{3} + 2\sqrt{2} - 3 - \sqrt{3} - \sqrt{3} - 1}{2}$$

$$= \frac{2\sqrt{2}\sqrt{3} + 2\sqrt{2} - 4 - 2\sqrt{3}}{2}$$

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